

# Corporate Yield Spreads and Bond Liquidity

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# Corporate Yield Spreads and Bond Liquidity

## **Abstract**

We examine whether liquidity is priced in corporate yield spreads. Using a battery of liquidity measures covering over 4000 corporate bonds and spanning investment grade and speculative categories, we find that more illiquid bonds earn higher yield spreads; and that an improvement of liquidity causes a significant reduction in yield spreads. These results hold after controlling for common bond-specific, firm-specific, and macroeconomic variables, and are robust to issuers' fixed effect and potential endogeneity bias. Our finding mitigates the concern in the default risk literature that neither the level nor the dynamic of yield spreads can be fully explained by default risk determinants, and suggests that liquidity plays an important role in corporate bond valuation.

## Introduction

A number of recent studies (Collin-Dufresne, Goldstein, and Martin, 2001, and Huang and Huang, 2003) indicate that neither levels nor changes in the yield spread of corporate bonds over treasury bonds can be fully explained by credit risk determinants proposed by structural form models. Illiquidity is acknowledged as a possible explanation for the failure of these models to more properly capture the yield spread variation (Longstaff, Mithal, and Neis, 2004). Yet much of the current literature abstracts from liquidity's influence (Elton, Gruber, Agrawal, and Mann, 2001), focuses on aggregate liquidity proxies (Grinblatt, 1995, Duffie and Singleton, 1997, Collin-Dufresne et al., 2001, and Campbell and Taksler, 2003) or simply assumes that the unexplained portion of the yield spread is liquidity based (Duffee, 1999). This paper attempts to fill this void by comprehensively assessing bond-specific liquidity for a broad spectrum of corporate investment grade and speculative grade bonds and by examining the association between bond-specific liquidity estimates and corporate bond yield spreads.

The notion that investors demand a liquidity premium for illiquid securities dates back to Amihud and Mendelson (1986). Lo, Mamaysky, and Wang (2004) further argue that liquidity costs inhibit the frequency of trading. Because investors cannot continuously hedge their risk, they demand an ex-ante risk premium by lowering security prices. Therefore, for the same promised cash flows, less liquid bonds will be traded less frequently, have lower prices, and exhibit higher yield spreads. Thus, the theoretical prior is that liquidity is expected to be priced in yield spreads. We investigate bond-specific liquidity effects on the yield spread using three separate liquidity measures. These include the bid-ask spread, the liquidity proxy of zero

returns, and a liquidity estimator based on a model variant of Lesmond, Ogden, and Trzcinka (1999). We find that liquidity is indeed priced in both levels and changes of the yield spread.

Contemporaneous studies by Longstaff et al. (2004) and Ericsson and Renault (2002) also relate corporate bond liquidity to yield spreads. However, Longstaff et al. (2004) focus only on 68 issuers that have liquid default-swap trading data, leaving some doubt as to the generality of the results for the larger universe of corporate bonds. Ericsson and Renault (2002) focus on a theoretical model and they simply use a new issue dummy as their empirical bond-specific liquidity measure. However, this liquidity proxy will not shed light on the liquidity difference spanning corporate bonds, nor provide liquidity measures for more mature bonds. We provide extensive bond-specific liquidity measures for over 4000 corporate bonds spanning investment and speculative grade categories over a nine year period allowing for a more comprehensive assessment of the relation between liquidity and yield spreads.

Historically, the lack of credible information on spread prices<sup>1</sup> or bond quotes has been a major impediment in the analysis of liquidity (Goodhart and O'Hara, 1997) and liquidity's impact on yield spreads. We employ *Bloomberg* and *Datastream* to provide our three liquidity estimates. Among them, the bid-ask spread is arguably the most demonstrable measure of liquidity costs, while the percentage of zero returns is increasingly used as a liquidity proxy in

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<sup>1</sup> Liquidity's importance is well recognized by academics, regulators, and bond traders. Arthur Levitt, as the Chairman of the Securities and Exchange Commission, notes that "the sad truth is that investors in the corporate bond market do not enjoy the same access to information as a car buyer or a home buyer or, I dare say, a fruit buyer. Improving transparency is a top priority for us" (*Wall Street Journal*, 9/10/1998). Greg Ip of the *Wall Street Journal* notes that "the bond market's biggest worry these days isn't default or interest rates. It's illiquidity that is crippling the very workings of the market" (*Wall Street Journal*, 10/19/1998). Reflecting on bond liquidity concerns, the NASD has recently instituted TRACE (Trade Reporting and Compliance Engine) which provides real-time quote estimates for 4200 corporate bond issues (*Wall Street Journal*, 3/14/2003).

a host of empirical studies.<sup>2</sup> Despite the clear intuition surrounding the zero return proxy, it is a noisy measure of liquidity, since it is the combination of a zero return and the simultaneous movement of bond price determinants that more properly estimates liquidity costs, not the lack of price changes per se.

To more properly capture this notion, we employ the limited dependent variable model proposed by Lesmond, Ogden, and Trzcinka (1999) (hereafter, LOT) to obtain an alternative liquidity estimate.<sup>3</sup> The premise of the LOT model is that, while the true value of the bond is driven by many stochastic factors, measured prices will reflect new information only if the information value of the marginal trader exceeds the total liquidity costs. This implies that a liquidity cost threshold exists for each bond, which is equivalent to the minimum information value for a trade. Within the liquidity cost threshold, the probability of observing a zero return is higher than outside the liquidity cost threshold. We use a maximum likelihood method to jointly estimate the risk factors related to market-wide information and the upper and lower liquidity thresholds that, taken as a whole, represent round-trip liquidity costs.

We find a significant association between corporate bond liquidity and the yield spread with each of the three liquidity measures. Depending on the liquidity measure, liquidity alone can explain as much as 7% of the cross-sectional variation in bond yields for investment grade bonds,

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<sup>2</sup> Theoretically, it is well known that in the presence of transaction costs, investors will trade infrequently (Constantinides, 1986), and thus the magnitude of the proportion of zero returns is representative of illiquidity. Empirically, this measure has been found to be an effective liquidity measure in the U.S. equity market (e.g., Lesmond, Schill, and Zhou, 2004) and in the emerging market for equities where the lack of liquidity-related information remains a challenge (e.g., Bekaert, Lundblad, and Campbell, 2003.)

<sup>3</sup> Lesmond et al. (1999) and Lesmond (2004) find that this method works well for equity markets, as evidenced by an 80% correlation between the LOT liquidity estimate and the bid-ask spread plus commissions. The proposed LOT model does not rely on the use of bid-ask spread prices; instead, it uses only daily closing returns to estimate liquidity costs. This method is also a natural extension of Glosten and Milgrom (1985), who illustrate that trades will occur when the information value exceeds the transaction costs defined by the bid-ask spread.

and 22% for speculative grade bonds. Using the bid-ask spread as the measure, we find that one basis point increase in bid-ask spread is related to 0.42 basis point increase in the yield spread for investment grade bonds, and 2.30 basis point increase for speculative grade bonds. Using either the bid-ask spread or the LOT estimate, the liquidity effect remains significant even after we control for general yield spread factors such as credit rating, maturity, and the amount outstanding; the tax effect (Elton et al., 2001); the equity volatility (Merton, 1974, and Campbell and Taksler, 2003); the accounting variables of Campbell and Taksler; and the macroeconomic variables of Collin-Dufresne et al. (2001). The results are robust to issuer fixed effects and potential endogeneity in yield spreads, liquidity, and credit ratings. The results extend to the zero return liquidity proxy, but are most robust for investment grade bonds.

Extending the study to changes in yield spreads, we again find a liquidity influence. Under all three liquidity measures, an increase in illiquidity is significantly and positively associated with an increase in yield spreads regardless of controlling for changes in credit rating, macro-economic influences, or firm-specific factors.

This paper contributes to the growing debate over bond market liquidity and corporate yields. First, in the credit risk literature, it is common to assume that the yield spread, as a whole, represents default risk. Practitioners frequently draw conclusions regarding default probability from yield spreads. Our findings imply that this approach is inappropriate, as the liquidity component in the yield spread is not directly related to default risk. Our results also mitigate the concern that the yield spread overstates the default probability (e.g., Elton et al., 2001, and Huang and Huang, 2003). Additionally, the high consistency between the traditional

model-independent measure, the bid-ask spread, and the model-dependent measure, the LOT estimate, suggests that the latter, making use of return data only, can be an effective tool in bond liquidity studies. This is particularly meaningful for illiquid bonds where the lack of liquidity-related information is common.

The paper is organized as follows. Section 1 introduces the liquidity measures and their summary statistics. Section 2 presents model validation tests, the consistency among the liquidity measures, and initial tests on the relation between liquidity and the yield spread. Section 3 studies the relation between liquidity levels and yield spread levels. Section 4 presents test results of changes in liquidity and changes in the yield spread. Section 5 concludes.

## **1. Liquidity Measures**

The literature provides a menu of measures for estimating liquidity. The most demonstrable measure is the bid-ask spread, but the spread is not always available for all bonds or for all time periods. This is especially true for thinly traded bonds or off-the-run bonds. Additionally, because our data is hand-collected, our quote information is gathered only on a quarterly basis resulting in a less precise measure of liquidity. This is especially true if only a single quarterly quote is available for the bond over an annual trading period.

Lesmond et al. (1999) introduce an alternative indirect method for estimating liquidity based on the occurrence of zero returns. Bekaert et al. (2004) show that zero returns themselves are a reasonable liquidity proxy. The LOT measure is a comprehensive estimate of liquidity by including the spread and other costs that may impinge on informed trade, such as commission costs, opportunity costs, and price impact costs. The maintained hypothesis is that the marginal



trader will trade only if the value of the information exceeds the marginal costs. If trading costs are sizeable, Lesmond et al. (1999) argue that zero return days will occur more frequently because new information must accumulate longer, on average, before informed trade affects price. They show that the LOT estimate is a more accurate measure of the underlying liquidity costs than is the percentage of zero returns because the LOT measure extracts more information from the return generating process.

A potential theoretical drawback of the LOT model is that it requires a return generating model for bonds which the literature has yet to definitively prescribe. A practical limitation is that the LOT model requires some zero returns to estimate liquidity's effect on the price. For on-the-run bonds or bonds offered mid-year, the sequence of prices may not reveal any zero returns invalidating the LOT estimate. Conversely, too many zero returns (i.e. greater than 85% over the estimation period) also makes this measure inestimable. However, both the zero return liquidity proxy and the LOT liquidity measure are presumed to be positively related to the bid-ask spread.

Because of the strengths and weaknesses of each measure, we employ all three estimators to determine the relation between corporate bond yield spreads and liquidity. This will not only increase robustness, but also shed light on the relative power of each liquidity measure. If we find that all three liquidity measures lead to consistent inferences, then we can take comfort in using the other two measures in situations where the bid-ask spread is not available. Bekaert et al. (2003) is a case in point when they study the equity liquidity in emerging markets.

### 1.1 The bid-ask spread

Data on the quarterly bid-ask quotes are hand-collected from the *Bloomberg Terminals*. Most quotes are available only from 2000 to 2003. For each quarter, we calculate the proportional spread as the ask minus the bid divided by the average bid and ask price. The bond-year's proportional bid-ask spread is then calculated as the average of the quarterly proportional spreads. To include as many bonds as possible, we compute the annual proportional spread as long as there is at least one quarterly quote for the year. The bid-ask quotes recorded are the *Bloomberg Generic Quote* which reflects the consensus quotes among market participants.

### 1.2 The percentage zeros and the LOT model

The LOT measure of informed trading utilizes only daily bond returns to estimate bond-level liquidity costs. The effect of liquidity is observable through the incidence of zero returns. *Datastream* is used to provide prices, which, in turn, uses Merrill Lynch as the data source for the price across all market makers for the bond. This feature will underestimate the number of zero returns for each bond issue as the probability of observing a zero return is decreasing with increasing numbers of market makers. Given that our model is predicated on days with no price changes, we will understate our estimate of bond-specific liquidity costs, biasing against our liquidity hypothesis. We choose the start date of 1995 since daily prices are more regularly available through *Datastream* only after 1995. The data span a nine-year period ending in 2003.

We record the clean, non-matrix price of each bond on a daily basis, deleting prices that deviate more than 50% from the prior day's price. We separate the data into bond-years; that is,

using daily data for each bond within each year, we jointly estimate the bond’s return generating function and liquidity costs applicable to that year. This allows time-series variations in the bond liquidity estimates to be adequately represented.

To price corporate bonds, we extend the Lesmond et al. (1999) methodology to a two-factor model. (Appendix A shows the theoretical basis for this approach.) The two factors are the interest rate and the equity market return, reflecting the fact that a corporate bond is a hybrid between a risk free bond and equity. Following Jarrow (1978), we scale all risk coefficients by duration to obtain stable estimation coefficients. The return generating process is then given as:

$$R_{j,t}^* = \beta_{j1} \text{Duration}_{j,t} * \Delta R_{ft} + \beta_{j2} \text{Duration}_{j,t} * \Delta \text{S\&P Index}_t + \epsilon_{j,t}. \quad (1)$$

The term  $R_{j,t}^*$  represents the unobserved “true” bond return for bond  $j$  and day  $t$  that investors would bid given zero transaction costs.  $\Delta R_{ft}$  is the daily change in the ten-year, risk-free interest rate. Following Cornell and Green (1991),  $\Delta \text{S\&P Index}$  is the daily return in the Standard & Poor’s 500 index.<sup>4</sup>

Amihud and Mendelson (1986, 1987) develop a framework in which the intrinsic value of a firm differs from its observed value. Amihud and Mendelson (1986) attribute this difference to a liquidity premium that requires higher cost assets to be priced lower to compensate investors for liquidity costs. Extending Amihud and Mendelson (1986) to fixed income securities, liquidity effects on bond returns can be stated as:

$$R_{j,t} = R_{j,t}^* - \alpha_{i,j}, \quad (2)$$

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<sup>4</sup> We also estimated the model using the Fama-French (1993) bond factors in the objective function. The results are largely invariant to this specification.

where  $R_{j,t}$  is the measured return,  $\alpha_{2,j}$  is the effective buy side cost, and  $\alpha_{1,j}$  is the effective sell side cost for bond  $j$ . Thus, the desired return and the measured return are related, but only after taking transaction costs into account. The effect of liquidity on bond prices is then modeled by combining the objective function with the liquidity constraint as:

$$R_{j,t}^* = \beta_{j1} \text{Duration}_{j,t} * \Delta R_{ft} + \beta_{j2} \text{Duration}_{j,t} * \Delta \text{S\&P Index}_t + \epsilon_{j,t}. \quad (3)$$

where:

$$\begin{aligned} R_{j,t} &= R_{j,t}^* - \alpha_{1,j} & \text{if} & & R_{j,t}^* < \alpha_{1,j} & \text{and} & \alpha_{1,j} < 0 \\ R_{j,t} &= 0 & \text{if} & & \alpha_{1,j} \leq R_{j,t}^* \leq \alpha_{2,j} & \\ R_{j,t} &= R_{j,t}^* - \alpha_{2,j} & \text{if} & & R_{j,t}^* > \alpha_{2,j} & \text{and} & \alpha_{2,j} > 0 \end{aligned}$$

The resulting log-likelihood function is stated as:

$$\begin{aligned} \text{LnL} = & \\ & \sum_1 \text{Ln} \frac{1}{(2\pi\sigma_j^2)^{1/2}} - \sum_1 \frac{1}{2\sigma_j^2} (R_j + \alpha_{1,j} - \beta_{j1} \text{Duration}_{j,t} * \Delta R_{ft} - \beta_{j2} \text{Duration}_{j,t} * \Delta \text{S\&P Index}_t)^2 \\ & + \sum_2 \text{Ln} \frac{1}{(2\pi\sigma_j^2)^{1/2}} - \sum_2 \frac{1}{2\sigma_j^2} (R_j + \alpha_{2,j} - \beta_{j1} \text{Duration}_{j,t} * \Delta R_{ft} - \beta_{j2} \text{Duration}_{j,t} * \Delta \text{S\&P Index}_t)^2 \\ & + \sum_0 \text{Ln}(\Phi_{2,j} - \Phi_{1,j}), \end{aligned} \quad (4)$$

where  $\Phi_{i,j}$  represents the cumulative distribution function for each bond-year evaluated at  $(\alpha_{i,j} - \beta_{j1} \text{Duration}_{j,t} * \Delta R_{ft} - \beta_{j2} \text{Duration}_{j,t} * \Delta \text{S\&P Index}_t) / \sigma_j$ .  $\sum_1$  (region 1) represents the negative nonzero measured returns,  $\sum_2$  (region 2) represents the positive nonzero measured returns, and  $\sum_0$  (region 0) represents the zero measured returns. Maddala (1983) and Lesmond et al. (1999) outline the estimation procedure.

For purposes of liquidity estimation, we focus only on the  $\alpha_{2,j}$  and  $\alpha_{1,j}$  estimates. Taken in difference form,  $\alpha_{2,j} - \alpha_{1,j}$ , represents the liquidity effects on bond returns related to round-trip transaction costs.

Implicitly, our model assumes that information motivates trade in bonds and that information is efficiently impounded into bond prices. This assumption finds support from Hotchkiss and Ronen (2002) who conclude that the informational efficiency of bond prices is similar to that of the underlying equity. The marginal trader is assumed to assess the value of information before deciding to trade relative to the expected liquidity costs. The marginal trader with the highest net difference between the value of information and transaction costs will drive price movements.<sup>5</sup> We do not impose any particular assumptions on whether the marginal investor possesses public or private information; rather, we assume that prices should rationally reflect the costs of trade relative to the information value of the trade. Unanticipated public information, noise trades, or trades of idiosyncratic nature will not be priced in a rational asset pricing framework and will only be captured, on average, in the error term.

### *1.3 Yield spreads and corporate information*

We examine over 4000 U.S. corporate bonds. *Datastream* is used to provide yield spreads and bond characteristics. We use the *Fixed Income Securities Database* to provide up-to-date credit ratings for each bond, and when unavailable we use *Standard and Poor's* rating on *Datastream*. We delete bonds not rated by either S&P or the *Fixed Income Securities Database*. Finally, we use the Compustat Annual Industrial database to collect all firm-level data for both active and inactive firms to minimize any survivorship bias in the liquidity determinant and yield spread regressions.<sup>6</sup> Each variable is collected in the year prior to the yield spread measurement. The

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<sup>5</sup> The LOT model is consistent with the Kyle (1985) model. Specifically, Kyle assumes that the market maker is risk neutral and allows for the market being composed of three trader types: informed, uninformed, and the market maker. The LOT model is predicated on trades made by the marginal trader who could be informed, uninformed, or even the market maker.

<sup>6</sup> We collect the operating income after depreciation (item 178) and the interest expense (item 15) to determine

equity volatility is estimated using 252 daily returns (from the CRSP file) for the year prior to the bond liquidity estimate. The bond volatility is estimated similarly using bond prices.

## 2. Preliminary Findings

### *2.1 Summary statistics*

Table 1 contains the summary statistics segregated by maturity levels and credit ratings. Within each panel there are two sets. The first set relates all the bond information for a matching sample of zero returns and the LOT estimate, while the second presents information for a matching sample of zero returns, the LOT estimate and the bid-ask spread. Several observations are apparent. First, liquidity costs are demonstrably higher for speculative grade bonds than for investment grade bonds. In particular, we observe a significant increase in the percentage of zero returns and the size of the LOT estimate of liquidity while moving from investment grade to speculative grade bonds. This is matched with a similar increase in the bid-ask spread.<sup>7</sup> Not surprisingly, yield spreads also increase markedly across these bond categories. For the matched sample of all three liquidity measures, the trend of each liquidity measure appears to match the underlying credit rating. Namely, for investment grade bonds, moving from AA bonds to BBB bonds we observe increasing transaction costs. However, for speculative grade bonds, the trend of increasing liquidity costs with decreasing credit worthiness,

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the pre-tax interest coverage. For the operating income to sales we collect the firm's operating income before depreciation (item 13) divided by the net sales (item 12). We use two definitions for debt: total long-term debt (item 9) divided by total assets (item 6), and total long-term debt plus debt in current liabilities (item 34) plus short-term borrowings (item 104) divided by total liabilities (item 181) plus market capitalization.

<sup>7</sup> We emphasize that, while the general trends are similar, the LOT liquidity costs do not necessarily need to agree with the bid-ask spread in magnitude. The LOT estimates are derived from the investors' trading decision, which incorporates all relevant liquidity related costs. The marginal traders' reservation price will then reflect all these relevant costs which could include commission costs, credit spread costs, and search costs, in addition to the bid-ask spread.

is only observed for the LOT measure and the bid-ask spread. The percentage of zero returns appears to be a weaker proxy for liquidity.

Second, liquidity costs increase moving from short to long maturity bonds, consistent with an investment horizon argument offered by Amihud and Mendelson (1991) or the return volatility arguments of Chakravarty and Sarkar (1999).

Finally, yield spreads generally increase (decrease) with maturity for investment (speculative) grade bonds. Merton (1974) shows that corporate yield spreads can either increase or decrease with maturity depending on the risk of the firm. Investment grade issuers face upward sloping yield spreads while speculative grade issuers face flat or downward sloping yield spreads. Helwege and Turner (1999) find that within the same speculative credit rating category, the safer firms tend to issue longer term bonds, which causes the average yield spread to decline with maturity.

## *2.2 Model validation*

Even though the proportion of zero returns and the LOT estimate both stem from the premise that liquidity costs inhibit trade, the LOT estimate is a less noisy measure because it incorporates the covariation between the zero returns and the market movement of the bond price determinants. To verify this point, we first perform a model specification check, by investigating whether the LOT model helps to recover intuitive beta coefficients on the systematic risk factors. These coefficients are then compared to a naive asset pricing model without liquidity cost considerations.

If the model is correctly specified, we would expect several patterns to appear. First, the interest rate coefficient should be negative. However, moving from high-grade to low-grade bonds, this relationship is expected to become weaker (Schultz, 2001). Second, the equity return coefficient should be positive for low-grade bonds (Cornell and Green, 1991). Intuitively, a positive equity return, signaling an improvement in the firm's business operation, will have a positive effect on the bond return. However, the effect of the equity return on high-grade bonds is not clear. On the one hand, a positive equity return might increase bond prices, as in the low-grade bond case. On the other hand, the positive equity return might be caused by capital flows from the corporate bond market into the equity market, in which case a negative return on corporate bonds is expected.<sup>8</sup>

The estimation results are summarized in Panel A of Table 2. A comparison of the LOT results with those of the naive OLS model provides a clear indication of the influence that zero returns have on the estimation results. The LOT model's interest rate estimates are mostly negative and significant, while the interest rate influence is decreasing with decreasing bond ratings, all as expected. In sharp contrast, the naive OLS model produces interest rate estimates that are largely insignificant from zero. In addition, the interest rate effect has no apparent trend with bond rating, contrary to common beliefs.

The falloff in interest rate influence for the LOT model is offset by a concomitant increase in the S&P500 equity return influence, especially for speculative grade bonds. Also evident is

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<sup>8</sup> Kwan (1996) finds a positive equity return coefficient for investment grade bonds. Cornell and Green (1991) find that, when both the interest rate and the S&P500 equity return are considered, the sign of equity return coefficient changes from positive to negative for the period 1977 to 1989.



the switch in sign for the S&P500 coefficient from investment grade to speculative grade bonds. This would indicate that signaling effects prevail in the case of speculative grade bonds, while substitution effects prevail for investment grade bonds. Similar, but more muted patterns are apparent for the naive OLS model’s estimates.

### *2.3 Bid-ask spread tests*

We provide further evidence on the consistency of the three liquidity measures. In particular, we regress the bid-ask spread separately on the other two liquidity measures controlling for other liquidity determinants as follows:

$$\text{Bid-Ask}_{it} = \eta_0 + \eta_1 \text{Liquidity}_{it} + \eta_2 \text{Maturity}_{it} + \eta_3 \text{Age}_{it} + \eta_4 \text{Amount Outstanding}_{it} \\ + \eta_5 \text{Bond Rating}_{it} + \eta_6 \text{Bond Volatility}_i + \eta_7 \text{Bond Rating Dummy} + \epsilon_t$$

The subscript “it” refers to bond i and year t. Liquidity refers to either the proportion of zero returns or the LOT estimate. The liquidity determinants are chosen according to Garbade and Silber (1979), Sarig and Warga (1989), Chakravarty and Sarkar (1999), Stoll (2000), Schultz (2001), and Brandt and Kavajecz (2003). Bond rating proxies for default risk. For the overall regressions, bond ratings are assigned a cardinal scale ranging from one for AAA rated bonds to seven for CCC to D rated bonds. Panel B of Table 2 presents the results.

For investment grade bonds, the LOT liquidity estimate alone explains 6.39% of the cross-sectional variation in the bid-ask spread, while the percentage of zero returns explains 6.82% of the cross-sectional variation in the bid-ask spread. In comparison, Schultz (2001) reports an  $R^2$  of 3.43% in regressions on all microstructure trading cost determinants for investment grade bonds. Both the LOT estimate and the percentage of zero returns remain

positively and significantly related to the bid-ask spread when other variables are included.<sup>9</sup> Similar results can be seen for speculative bonds, but only for the LOT model estimate. In particular, the proportion of zeros is insignificant without the control variables, but becomes significant after including them in the regression. The percentage of zero returns appears to suffer more from specification error bias than does the LOT measure. This is to be expected given that the LOT measure extracts more information than is provided by the percentage of zero returns.

#### *2.4 Initial yield spread and liquidity tests*

We now test the relation between the yield spread and the three liquidity estimates. To provide a consistent comparison we match the bid-ask spread sample to the available liquidity estimates. As shown in Panel C of Table 2, for investment grade bonds all three liquidity estimates are positively and significantly associated with the underlying yield spread. The LOT measure and the bid-ask spread provide almost identical power in explaining the cross-sectional variation in the yield spread, with a reported  $R^2$  of approximately 7.3%. The percentage of zero returns explains almost 6% of the cross-sectional variation in the yield spread.

For speculative bonds, only the bid-ask spread and the LOT measure are significantly associated with the underlying yield spread. The LOT measure explains 7.39% of the cross-sectional variation in the yield spread, while the bid-ask spread explains only 0.86% of the cross-sectional variation in the yield spread.

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<sup>9</sup> Although not reported, we also include the log scaled equity volatility in the regression and find it to be *insignificantly* associated with the bid-ask spread.

### 3. Liquidity Effects on Yield Spread Levels

Many theoretical models (e.g., Amihud and Mendelson, 1986) predict that investors demand higher expected returns for less liquid assets to compensate for the liquidity risk. This implies that, for the same cash flows in the future, less liquid assets will have lower prices. Because bond yield is a promised yield given known cash flows, the lower prices of less liquid bonds lead to higher bond yields and higher yield spreads, *ceteris paribus*. We test this theoretical prediction by investigating whether various liquidity proxies can explain yield spread levels.

#### *3.1 Regression tests of liquidity estimates and other yield spread determinants*

The following regression is specified with the yield spread as the dependent variable and the various yield spread determinants as independent variables:

$$\begin{aligned} \text{Yield Spread}_{it} = & \eta_0 + \eta_1 \text{Liquidity}_{it} + \eta_2 \text{Maturity}_{it} + \eta_3 \text{Amount Outstanding}_{it} \\ & + \eta_4 \text{Coupon}_{it} + \eta_5 \text{Treasury Rate}_t + \eta_6 \text{10Yr-2Yr Treasury Rate}_t + \eta_7 \text{EuroDollar}_t + \eta_8 \text{Volatility}_{it} \\ & + \eta_9 \text{Bond Rating}_t + \eta_{10} \text{PreTax Coverage Dummy}_{it} + \eta_{11} \text{Operating Income/Sales}_{it} \\ & + \eta_{12} \text{Debt/Assets}_{it} + \eta_{13} \text{Debt/Capitalization}_{it} + \epsilon_t \end{aligned}$$

The subscript “it” refers to bond *i* and year *t*. Liquidity refers to the bid-ask spread, the proportion of zero returns, or the LOT estimate. The choice of yield spread determinants is largely based on Elton et al. (2001) and Campbell and Taksler (2003).<sup>10</sup> We measure the incremental influence of the pretax coverage using the procedure outlined in Blume, Lim, and MacKinlay (1998). In addition, we include three macroeconomic variables associated with the yield spread. These are the one-year Treasury rate, the difference between the 10-year and

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<sup>10</sup> We exclude the additional equity market index considered by Campbell and Taksler (2003) because of potential endogeneity problems given that the LOT estimate includes the market return from the S&P500 index.

2-year Treasury rates that describes the slope of the yield curve, and the difference between the 30-day Eurodollar and 3-month Treasury bill rate that controls for other potential liquidity effects on corporate bonds relative to Treasury bonds.

We present two separate regressions for each liquidity estimate. The first uses only the bond-specific information yielding a larger sample, while the second incorporates the corporate and market information yielding a smaller sample. The sample for each liquidity measure differs due to the estimation limitations for each measure. The percentage of zero returns is the most comprehensive sample because it only requires the daily bond prices. As a practical matter, The LOT sample comprises more off-the-run bonds than does the bid-ask spread sample, but the bid-ask spread sample comprises more on-the-run bonds than does the LOT sample.

The most telling finding is the consistent significance of the liquidity variable regardless of the specification used to define liquidity, regardless of the specification used for the yield spread determinants, or regardless of investment grade or speculative grade categories. All these liquidity measures are positively related to the yield spread in all scenarios, for both investment grade and speculative grade bonds, even after we control for extensive bond-specific, firm-specific, and macroeconomic variables. The liquidity coefficients are highly significant (at 1%) in every scenario, supporting our theoretical prior that liquidity is priced in the yield spreads.

The interpretation of the magnitude of the liquidity influence varies depending on the liquidity measure. For investment grade bonds, the LOT measure would predict an incremental 0.21 basis point increase in the yield spread for a one basis point increase in liquidity costs,

while the bid-ask spread would predict an incremental 0.42 basis point increase in the yield spread for a one basis point increase in the bid-ask spread. The coefficient for bond rating is 20 basis points, regardless of the LOT measure or the bid-ask spread liquidity measure, which means that for each grade drop in bond rating (e.g., from BBB+ to BBB), the yield spread will increase by 20 basis points. The incremental effect of maturity on the yield spread is significant, but only one basis point.

For speculative grade bonds, focusing on the full accounting variable regressions, the LOT measure would predict an incremental 0.82 basis point increase in the yield spread for a one basis point increase in liquidity costs, while the bid-ask spread would predict an incremental 2.29 basis point increase in the yield spread for a one basis point increase in the bid-ask spread.

It may be noted that the maturity coefficient is generally positive for investment grade bonds and negative for speculative grade bonds. For investment grade bonds, longer maturities are often noted to be associated with increased yield spreads (Campbell and Taksler, 2003), consistent with the positive sign for maturity. For speculative grade bonds, Helwege and Turner (1999) argue that better quality firms are able to issue bonds with longer maturity, causing a negative relation between the yield spread and maturity for these bonds.

At the bottom of Table 3 we report the regression of yield spread on each liquidity measure alone using the full sample whenever the measure is available. For each measure, we also regress the yield spread on bond rating alone for that sample as a comparison. For investment grade bonds, liquidity alone explains from 2.12%, for the bid-ask spread, to 7.57%, for the LOT estimate, of the cross-sectional variation in the yield spread. In comparison, for the same sample,

bond rating alone explains 15.20% of the cross-sectional variation of yield spread for the LOT sample and 20.12% for the bid-ask spread sample. For speculative bonds, the bid-ask spread alone explains 7.49% of the yield spread variation while the LOT liquidity measure explains 21.83% of the yield spread variation.

### *3.2 Issuer fixed-effects regressions*

We perform an issuer fixed-effects regression to control for issuer influences on yields because a small set of companies may dominate the bond market. For instance, Ford Motor Company's bonds comprise almost 10% of the entire bond market. As in the levels regression tests, we use separate samples for each liquidity measure to allow for different bond characteristics. This results in approximately 1100 issuers for investment grade bonds and 220 issuers for speculative grade bonds. However, approximately only 300 issuers have complete accounting information for investment grade bonds and approximately only 90 issuers have complete accounting information for speculative grade bonds. Table 4 presents the results.

We observe the same, consistent result using either the bid-ask spread or the LOT liquidity estimate. Liquidity is positively and significantly associated with the yield spread regardless of bond grade, even after controlling for bond-specific, firm-specific, and macroeconomic variables. The coefficients are highly significant at 1%. Note that the proportion of zero returns is significantly positive (at 1%) for both investment grade bonds and for speculative grade bonds when the accounting variables are not included, but is only significant at 10% when the firm-level variables are included. In other words, while all liquidity measures lead to the same conclusion, the case for the proportion of zero returns is slightly weaker, consistent with the notion that the

proportion of zero returns is a relatively noisy measure of liquidity.

### *3.3 Simultaneous equation regressions*

Every liquidity measure, whether based on observable bid-ask spreads or new estimable measures, could contain information about the credit quality of a bond, and thus could affect the yield through the credit-risk channel. This would make it difficult to interpret the main results purely in terms of liquidity costs. Much of the liquidity costs are due to adverse selection under asymmetric information. For a typical corporate bond, asymmetric information on its credit quality (rather than on interest rate) is the main reason for adverse selection costs. Intuitively, one expects that bonds with lower credit quality should have a more severe adverse selection problem, *ceteris paribus*. So higher liquidity costs could mean a lower credit quality, which should lead to higher yield spreads. In addition, Campbell and Taksler (2003) note that bond ratings may be contemporaneously incorporating the observed firm-level accounting characteristics. Rating agencies may also absorb market information through the observed yield spread as well as macro-economic information when assigning a credit rating.

To control for the potential endogeneity problems arising from the contemporaneous measurement of the yield spread, liquidity costs, and the credit rating, we perform a simultaneous regression using three equations representing each of the potentially endogenous variables. The system of equations is stated as follows:

$$\begin{aligned} \text{Yield Spread}_{it} = & \eta_0 + \eta_1 \text{Liquidity}_{it} + \eta_2 \text{Maturity}_{it} + \eta_3 \text{Coupon}_{it} \\ & + \eta_4 \text{Treasury Rate}_t + \eta_5 \text{10Yr -2Yr Treasury Rate}_t + \eta_6 \text{EuroDollar}_t + \eta_7 \text{Volatility}_{it} \\ & + \eta_8 \text{Credit Rating}_t + \eta_9 \text{PreTax Coverage Dummy}_{it} + \eta_{10} \text{Operating Income/Sales}_{it} \\ & + \eta_{11} \text{Debt/Assets}_{it} + \eta_{12} \text{Debt/Capitalization}_{it} + \epsilon_t \end{aligned}$$

$$\begin{aligned} \text{Liquidity}_{it} = & \eta_0 + \eta_1 \text{Maturity}_{it} + \eta_2 \text{Age}_{it} + \eta_3 \text{Amount Outstanding}_{it} \\ & + \eta_4 \text{Credit Rating}_{it} + \eta_5 \text{Bond Volatility}_{it} + \eta_6 \text{Yield Spread}_{it} + \epsilon_t \end{aligned}$$

$$\begin{aligned} \text{Credit Rating}_{it} = & \eta_0 + \eta_1 \text{Treasury Rate}_{it} + \eta_2 \text{10Yr -2Yr Treasury Rate}_t \\ & + \eta_3 \text{PreTax Coverage Dummy}_{it} + \eta_4 \text{Operating Income/Sales}_{it} + \eta_5 \text{Debt/Assets}_{it} \\ & + \eta_6 \text{Debt/Capitalization}_{it} + \eta_7 \text{Yield Spread}_{it} + \epsilon_t \end{aligned}$$

The results are presented in Table 5. As is shown, the potential endogeneity bias does not affect the relation between liquidity and the yield spread for either investment grade or speculative grade bonds. The LOT liquidity estimate and the bid-ask spread liquidity measure remain significant at the 1% level for investment grade bonds, and they remain significant at the 5% level for speculative grade bonds. The percentage of zero returns is significant at the 5% level for investment grade bonds, but is insignificant for speculative grade bonds. We conclude that liquidity is priced in yield spreads even after the potential endogeneity bias is controlled; and that, again, the proportion of zero returns appears to be a less powerful liquidity measure.

#### 4. Liquidity Effects on the Yield Spread Changes

We conduct regression tests to study whether issue-specific liquidity changes are a determinant of yield spread changes. This test offers a glimpse into how the dynamics of liquidity are incorporated into yield spread changes. Econometrically, differencing the time-series removes autocorrelative influences that may cause spurious results due to time-series trends.



#### 4.1 Regression tests of changes in liquidity and yield spread determinants

We include a list of independent variables used in Collin-Dufresne et al. (2001) and Campbell and Taksler (2003). Unlike the levels specification, we use the unscaled pretax coverage because of the differencing operation. In addition, unlike Collin-Dufresne et al., we directly control for the default probability by using the changes experienced each year in the credit ratings for each bond. We believe this is a better control than using the change in the forward jump rate in the option market. The regression is stated as:

$$\begin{aligned}\Delta(\text{Yield Spread})_i = & \gamma_0 + \gamma_1\Delta(\text{Liquidity})_i + \gamma_2\Delta(\text{S\&P Rating})_i + \gamma_3\Delta(\sigma_E)_i + \gamma_4\Delta(\text{Treasury Rate})_i \\ & + \gamma_5\Delta(\text{10 yr - 2 yr Treasury Rate})_i + \gamma_6\Delta(\text{30 Day EuroDollar Rate})_i \\ & + \gamma_7\Delta(\text{PreTax Interest Coverage})_i + \gamma_8\Delta(\text{Operating Income/Sales})_i \\ & + \gamma_9\Delta(\text{LT Debt/Assets})_i + \gamma_{10}\Delta(\text{Total Debt/Market Cap})_i + \epsilon\end{aligned}$$

where,  $\Delta$  represents the first difference in each variable, for each bond  $i$ . The results are presented in Table 6.

As expected, a deterioration of bond quality (rating) is related to a significant increase in the yield spread. Similarly, a rise in interest rates leads to a reduction in the yield spread, especially for investment grade bonds (Duffee, 1998, and Longstaff and Schwartz, 1995). However, even after controlling for this and other factors, changes in liquidity are highly associated with changes in the yield spread, especially for the bid-ask spread and the LOT estimate. This is the case for both investment grade and speculative grade bond categories.

Adding the macro-variables and firm-specific accounting variables increases the explanatory power, but not at the expense of the liquidity variable which remains significant. The

conclusive result in Table 6 is the positive, significant coefficient for the liquidity change variable. Liquidity changes remain significantly associated with yield spread changes regardless of including bond-specific, firm-specific, or macro-level variables.

Economically, for investment grade bonds, a one basis point increase in LOT liquidity costs over time results in a 0.12 basis point increase in the yield spread, while a one basis point increase in the bid-ask spread over time results in a 0.29 basis point increase in the yield spread. The corresponding impact for speculative grade bonds are 0.61 basis points (LOT liquidity costs) and 2.46 basis points (bid-ask spread). Note that the coefficients for the liquidity variables are broadly consistent with those of Table 3.

At the bottom of Table 6 we report the regression of the change in the yield spread on the change in each liquidity measure alone using the full sample whenever the measure is available. For each measure, we also regress the change in the yield spread on the change in bond rating alone for that sample as a comparison. For investment grade bonds, the changes in the percentage of zero returns and the LOT liquidity measure explain more than 2.0% of the cross-sectional variation in the change of yield spread. For speculative bonds, changes in the LOT liquidity measure alone explains 16.89% of changes in the yield spread, while changes in the percentage zeros alone explains 5.97% of changes in the yield spread. Changes in the bid-ask spread alone have a relatively lower explanatory power for both categories of bonds.

#### 4.2 Simultaneous regression tests

To control for the potential endogeneity bias, we run a simultaneous system regression with the yield spread change and the change in each of the liquidity measure (respectively) as the endogenous variables. Unlike the levels test, we do not endogenize bond rating changes because changes in the credit rating are infrequent within the sample period, causing a limited dependent variable problem in the simultaneous system regression. Additionally, the equations for the bid-ask spread sample for speculative grade bonds were unidentified because of linear dependence between the macroeconomic variables. We therefore remove the Eurodollar variable to allow for system identification. Moreover, changes in maturity, age, and coupon are also excluded. The resulting simultaneous regression for yield spread changes is specified as:

$$\begin{aligned}\Delta(\text{Yield Spread})_i = & \eta_0 + \eta_1 \Delta(\text{Liquidity})_i + \eta_2 \Delta(\text{Treasury Rate})_i + \eta_3 \Delta(\text{10Yr -2Yr Treasury Rate})_i \\ & + \eta_4 \Delta(\text{EuroDollar})_i + \eta_5 \Delta(\text{Volatility})_i + \eta_6 \Delta(\text{Credit Rating})_i + \eta_7 \Delta(\text{PreTax Coverage})_i \\ & + \eta_8 \Delta(\text{Operating Income/Sales})_i + \eta_9 \Delta(\text{Debt/Assets}_i) + \eta_{10} \Delta(\text{Debt/Capitalization})_i + \epsilon\end{aligned}$$

$$\Delta(\text{Liquidity})_{it} = \eta_0 + \eta_1 \Delta(\text{Credit Rating})_i + \eta_2 \Delta(\text{Bond Volatility})_i + \eta_3 \Delta(\text{Yield Spread})_i + \epsilon$$

The results, presented in Table 7, can be summarized as follows. For the bid-ask spread or the LOT estimates, an increase of liquidity costs causes a significantly positive increase in yield spreads, for both the investment grade and the speculative grade bonds. For the proportion of zero returns, an increase of liquidity costs causes a significant increase in yield spreads for investment grade bonds, but not for speculative bonds. The results concerning the percentage of zero returns for the speculative grade bonds are consistent with the levels tests. On the whole, Table 7 indicates that our tests on changes in liquidity are robust to potential endogeneity bias.

## 5. Conclusions

We examine the association between corporate bond liquidity and yield spreads. To ensure robustness, we adopt two model-independent liquidity measures (the bid-ask spread and the proportion of zero returns) and a liquidity estimate from a model developed by Lesmond et al. (1999). We provide additional robustness checks to ensure that our liquidity measures are intuitively consistent and empirically sound.

We find that liquidity is a key determinant in yield spreads. This is found both in yield spread levels and changes over time. Liquidity is priced in yield spreads regardless of controlling for issuer fixed effects, potential simultaneity bias between credit ratings, liquidity, and yield spreads, or the commonly used yield spread determinants adopted by Campbell and Taksler (2003) and yield spread change determinants of Collin-Dufresne et al. (2001). The liquidity effects are apparent for both the investment grade and speculative grade bonds.

Our study adds to the literature in the following sense. Many prior studies simply assume that liquidity is a second order effect, or totally neglect its impact given the difficulties in estimating liquidity costs. The observation that bond yields exhibit significant liquidity effects alters our view of bond pricing and risk estimation. It mitigates the concern that the yield spread is “too high” to be explained by default risk alone (Elton et al., 2001 and Huang and Huang, 2003). Our results imply that the liquidity-related component must be taken into account when examining yield spreads.

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## Appendix A: The Return Generating Function

The bond price,  $B_t$ , by definition, is:

$$B_t = \sum_{n=T-t-k}^{T-t} C e^{-rn} + A e^{-r(T-t)},$$

where  $T$  is the maturity,  $k+1$  is the number of coupon payments remaining,  $C$  is the half-year coupon payment rate,  $A$  is the face value of debt, and  $r$  is the yield to maturity for  $k+1$  coupon payments remaining. We assume that  $r_t$  follows some unspecified stochastic process. By Ito's lemma we have:

$$dB_t = \frac{\partial B}{\partial r} dr + \frac{\partial B}{\partial t} dt + \frac{1}{2} \frac{\partial^2 B}{\partial r^2} \Lambda_t dt, \quad (A1)$$

where  $\Lambda_t$  is the square of the diffusion coefficients of  $r_t$  process. If  $r_t$  is a multivariate process, then  $\Lambda_t$  should also include the covariance terms. Therefore, from Equation (A1):

$$\frac{\partial B}{\partial r} = -D_t B_t, \quad (A2)$$

where  $D_t$  is the bond's duration. We can rewrite Equation (A2) as:

$$\frac{dB_t}{B_t} = -D_t dr + \frac{\left( \frac{\partial B}{\partial t} + \frac{1}{2} \frac{\partial^2 B}{\partial r^2} \Lambda_t \right)}{B_t} dt. \quad (A3)$$

Barring arbitrage, there exists some state price density process,  $\Lambda_t$ , such that:

$$d\Lambda_t = \mu_{\Lambda,t} dt + \sigma_{\Lambda,t}^T d\omega_t.$$

In equilibrium, the risky bond return should satisfy:

$$E_t \left[ \frac{dB_t}{B_t} \right] - r_t dt = -cov_t \left( \frac{dB_t}{B_t}, \frac{d\Lambda_t}{\Lambda_t} \right) = D_t cov_t \left( r_t, \frac{d\Lambda_t}{\Lambda_t} \right), \quad (A4)$$

where  $cov_t(dP_t/P_t, d\Lambda_t/\Lambda_t)$  is the instantaneous conditional covariance, and  $r_t = -\mu_{\Lambda,t}/\Lambda_t$  is the risk-free rate. We obtain the second equality above by using Equation (A3). Following the discrete time empirical literature, we further assume that the state price density is a linear function of both market equity return and long-term risk free bond return (e.g., Scruggs, 1998). This implies that:

$$E_t \left[ \frac{dB_t}{B_t} \right] = r_t dt + D_t \times \gamma_1 \times cov_t \left( r_t, \frac{dB_{l,t}}{B_{l,t}} \right) + D_t \times \gamma_2 \times cov_t \left( r_t, \frac{dM_t}{M_t} \right), \quad (A5)$$

where,  $\gamma_i$ ,  $i = 1, 2$  is the price of risk associated with the respective state variable,  $dB_{l,t}/B_{l,t}$  is long-term bond return, and  $dM_t/M_t$  is market equity return. In the empirical implementation, we will make the two adjustments. First, we only measure the proportional daily price change in  $dB_t/B_t$  and we will not consider daily accrued interest. The last condition means we will consider only clean prices. In summary, bond price changes will only be driven by long-term risk free bond returns and equity returns. We also assume the conditional covariances are constant.<sup>11</sup> This leads to the following specification for equation (1) in the text:

$$R_{j,t}^* = \beta_{j1} \times Duration_{j,t} \times \Delta R_{l,t} + \beta_{j2} \times Duration_{j,t} \times \Delta \text{S\&P Index}_t + \epsilon_{j,t}, \quad (1)$$

where  $R_{j,t}$  is the daily return for bond  $j$  that investors would bid given zero transaction costs,  $Duration_{j,t}$  is the bond's duration, and  $\Delta \text{S\&P Index}_t$  is daily S&P equity return.  $Duration_{j,t} \times \Delta R_{l,t}$  is the proportional bond return of a long-term risk free bond adjusted by the duration of the risky bond. The scaling of the market sensitivities by duration is consistent with Jarrow (1978).

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<sup>11</sup> This can be justified for two reasons. First, for each bond we split daily bond prices into separate years and estimate beta coefficients within the year. The coefficients can thus be treated as conditionally constant. Second, we assume that changes in duration for each bond within the year will capture some of the variation in beta coefficients.

**Table 1**

**Corporate Bond Summary Statistics**

We present liquidity and yield spread statistics for non-callable corporate bonds from 1995 to 2003 by three maturity categories. %Zeros is the percentage of zero returns for a given year adjusted for missing prices. LOT refers to the modified Lesmond et al. (1999) model's liquidity estimate. The bid-ask is the proportional spread derived from quarterly quotes from *Bloomberg*. To assign bond ratings, we use the *Fixed Income Securities Database*, and, when unavailable, the Standard & Poor's credit rating from *Datastream*. The yield spread is the difference between the bond yield and the yield of a comparable maturity treasury bond as determined from *Datastream*. Two separate samples for each maturity classification are presented. The first sample is restricted to only bonds with available LOT estimates, while the second sample is restricted to only bonds with available bid-ask spreads. bp stands for basis points and N stands for the sample size.

Short Maturity (1-7 years)							
Liquidity & Yield Spreads	S&P Credit Ranking						
	AAA	AA	A	BBB	BB	B	CCC to D
Zeros (%)	5.93	4.10	3.88	8.43	40.63	44.71	46.31
LOT (bp)	7.88	9.63	10.51	34.99	201.45	458.86	933.06
Yield Spread (bp)	84.06	96.91	129.34	252.09	575.58	1213.43	3949.55
N	87	336	1162	1234	333	167	119
Zeros (%)	3.20	3.35	3.33	7.80	42.77	44.00	51.09
LOT (bp)	5.83	8.18	9.82	34.40	191.23	335.63	868.59
Bid-Ask (bp)	24.51	26.02	25.82	31.01	54.26	58.76	77.00
Yield Spread (bp)	71.43	95.05	118.92	235.41	549.88	1247.23	3559.09
N	56	285	972	775	178	72	22
Medium Maturity (7-15 years)							
Liquidity & Yield Spreads	S&P Credit Ranking						
	AAA	AA	A	BBB	BB	B	CCC to D
Zeros (%)	9.79	12.59	10.61	11.94	36.99	38.71	34.96
LOT (bp)	24.28	47.26	57.74	70.29	259.34	342.50	941.84
Yield Spread (bp)	82.44	146.24	177.68	277.45	566.53	947.14	2887.47
N	49	120	539	730	152	78	44
Zeros (%)	10.36	8.34	6.62	8.91	42.40	38.96	18.04
LOT (bp)	25.00	36.17	36.82	51.45	266.11	272.96	282.84
Bid-Ask (bp)	49.52	36.57	38.20	44.22	54.65	60.44	180.35
Yield Spread (bp)	70.65	129.02	154.19	251.68	497.45	863.71	1619.04
N	37	67	386	394	76	32	9
Long Maturity (15-40 years)							
Liquidity & Yield Spreads	S&P Credit Ranking						
	AAA	AA	A	BBB	BB	B	CCC to D
Zeros (%)	7.53	9.75	10.39	8.68	29.13	31.67	41.00
LOT (bp)	59.34	83.65	79.40	66.57	252.14	284.81	1023.18
Yield Spread (bp)	133.81	152.25	183.76	242.16	437.69	681.44	2047.11
N	49	189	674	929	112	48	48
Zeros (%)	7.28	8.27	7.79	8.00	32.36	37.25	35.14
LOT (bp)	76.81	75.60	56.97	58.57	281.56	245.78	328.25
Bid-Ask (bp)	51.65	52.68	54.76	58.62	73.56	82.47	86.75
Yield Spread (bp)	113.65	142.83	172.21	236.89	457.97	623.45	2192.41
N	27	110	410	494	62	14	8

Table 2

Liquidity Measure Tests

Panel A reports coefficients on the risk free rate factor,  $\beta_{T-Bond}$ , and the equity market return factor,  $\beta_{Equity}$ , from, respectively, a naive OLS model and the modified Lesmond et al. (1999) model (LOT). The interest rate factor is expected to be negative for all bonds while the equity factor can be either positive or negative for investment grade bonds but positive for speculative grade bonds. N is the sample size for each bond rating. %Zeros is the percentage of zero returns for a given year adjusted for missing prices. LOT is the liquidity estimate from the Lesmond et al. (1999) model. Panel B reports the regression of the bid-ask spread on the other two liquidity measures, the percentage of zero returns, and the LOT estimate, and control for other liquidity determinants. Age and maturity are in years referenced from the year the bond was issued or its maturity date relative to the year being analyzed. The amount outstanding is the dollar amount of the bond that has not been redeemed and is log scaled. The bond volatility is log scaled. The bond ratings are numbered from one to 10 for investment grade bonds (S&P ratings, AAA to BBB-) and from one to 12 for speculative grade bonds (S&P ratings, BB+ to D). Panel C reports an OLS regression of the yield spread on each liquidity measure for a matched sample using the bid-ask as a basis. White's (1980) t-statistics are in parentheses. An \* denotes significance at the 1% level, while a † denotes significance at the 5% level.

Panel A: LOT Model and the Naive Model Coefficient Estimates

	S&P Rating	N	% Zeros	Limited Dependent Variable Model			Naive Model	
				LOT	$\beta_{T-Bond}$	$\beta_{Equity}$	$\beta_{T-Bond}$	$\beta_{Equity}$
Investment Grade	AAA	185	7.37*	0.0026*	-0.9077*	-0.0072*	-0.0515	-0.0055*
	AA	645	7.34*	0.0038*	-0.9127*	-0.0084*	0.0068*	-0.0064*
	A	2395	7.29*	0.0041*	-0.9395*	-0.0090*	-0.0223	-0.0068*
	BBB	2893	9.40*	0.0054*	-0.9047*	-0.0069*	-0.0487	-0.0040†
Speculative Grade	BB	597	37.55*	0.0225*	-0.5332*	-0.0001	-0.0450	-0.0019
	B	293	40.97*	0.0399*	0.4424	0.0171†	-0.1261	0.0127*
	CCC to D	211	42.74*	0.0955*	-0.1976	0.0885*	-0.0662	0.0341†

Panel B: Regression of the Bid-Ask Spread on Liquidity Measures

Variable	Investment Grade Bonds				Speculative Grade Bonds			
Intercept	0.0112* (103.18)	0.0059* (5.31)	0.0032* (129.10)	0.0051* (6.50)	0.0049* (26.06)	0.0043 (0.99)	0.0054* (26.96)	0.0069 (1.74)
LOT	<b>0.0442*</b> (9.81)	<b>0.0233*</b> (5.65)			<b>0.0440*</b> (5.16)	<b>0.0297*</b> (3.50)		
% Zeros			<b>0.0037*</b> (15.03)	<b>0.0027*</b> (11.73)			0.0007 (1.81)	<b>0.0017*</b> (3.80)
Maturity		0.0001* (10.59)		0.0001* (12.92)		0.0001* (4.02)		0.0001* (5.46)
Age		-0.0000 (0.34)		0.0000 (1.25)		0.0001 (1.67)		0.0001 (0.89)
Ln(Amt. Outstanding)		0.0001 (0.60)		0.0001† (2.34)		-0.0000 (0.14)		-0.0001 (0.16)
Ln(Bond Volatility)		0.0004* (12.15)		0.0003* (14.61)		0.0001 (1.47)		0.0002* (3.05)
Bond Rating		0.0001 (1.38)		0.0001 (1.49)		0.0002† (2.30)		0.0003* (2.81)
Sample Size	3970		6040		421		525	
% Adjusted R <sup>2</sup>	6.39	25.34	6.82	25.23	6.45	15.02	0.35	15.03

Panel C: Regression of the Yield Spread on Liquidity Measures

Variable	Investment Grade Bonds			Speculative Grade Bonds		
	Bid-Ask	LOT	% Zero	Bid-Ask	LOT	% Zero
Coefficient	<b>1.8246*</b> (17.70)	<b>0.3181*</b> (17.65)	<b>0.0239*</b> (15.76)	<b>1.7396†</b> (2.16)	<b>0.7804*</b> (5.88)	0.0014 (1.87)
N	3970			421		
% Adjusted R <sup>2</sup>	7.29	7.26	5.87	0.86	7.39	1.72

### Table 3

## Yield Spread Determinants and Liquidity Tests

The yield spread determinants are based on bond-specific effects (bond rating, amount outstanding, and maturity in years), macroeconomic variables (One-year Treasury note rate (T-Note), the difference between the 10-year and 2-year Treasury rates (Term Slope), and the 30-day Eurodollar rate minus the 3-month T-Bill Rate (Eurodollar)), and firm-specific operating characteristics (pre-tax interest coverage, operating income to sales, long-term debt to assets, and total debt to capitalization). The pretax interest coverage is further grouped into one of four categories according to Blume et al. (1998).  $\sigma_E$  is the equity volatility for each issuer. Investment grade bonds are numbered from one (AAA rated bonds) to 10 (BBB- rated bonds) Speculative grade bonds are numbered from one (BB+ rated bonds) to 12 (D rated bonds). The liquidity cost estimates are based on the modified LOT model, the percent zero returns, and the bid-ask spread. White's (1980) t-statistics are presented in parentheses. The last partition is a univariate regression of the yield spread on either liquidity or credit rating alone using only the bond-specific sample for each liquidity measure. An \* or a † signifies significance at the 1% or 5% level, respectively.

Variable	Investment Grade Bonds						Speculative Grade Bonds					
Intercept	0.1573*	0.1251	0.0696*	0.0902*	0.1737*	0.1408†	0.5696†	0.5397†	0.3232*	0.2784*	0.9056*	0.8242*
	(15.03)	(11.52)	(9.97)	(8.76)	(12.25)	(14.08)	(2.00)	(1.98)	(2.81)	(3.23)	(2.99)	(2.88)
LOT	<b>0.5122*</b>	<b>0.2166*</b>					<b>1.6757*</b>	<b>0.8213*</b>				
	(10.71)	(10.03)					(7.82)	(2.95)				
Bid-Ask			<b>0.4362*</b>	<b>0.4200*</b>					<b>2.7266*</b>	<b>2.2957*</b>		
			(5.65)	(5.20)					(4.99)	(4.69)		
% Zeros					<b>0.0255*</b>	<b>0.0138*</b>					<b>0.0600*</b>	<b>0.0521*</b>
					(12.94)	(8.84)					(5.25)	(3.10)
Maturity	0.0001	0.0001*	0.0001*	0.0001*	0.0001*	0.0001*	-0.0024*	-0.0021*	-0.0009*	-0.0106*	-0.0027*	-0.0032*
	(1.57)	(5.28)	(5.40)	(5.89)	(7.25)	(7.44)	(4.62)	(3.92)	(5.75)	(4.03)	(5.61)	(4.93)
Amount	0.0001	-0.0005	0.0003	-0.0008†	-0.0001	-0.0007*	-0.0071*	0.0005	-0.0004	0.0011	-0.0064†	0.0023
	(0.34)	(1.33)	(0.92)	(2.48)	(0.75)	(2.66)	(3.08)	(0.34)	(0.17)	(0.28)	(2.25)	(0.78)
Coupon	0.2074*	0.1141*	0.0013*	0.0009*	0.1828*	0.1078*	0.4895	0.4441†	0.0034*	0.0027*	1.3981*	1.2975†
	(10.30)	(6.28)	(11.09)	(5.48)	(12.45)	(7.36)	(1.52)	(2.13)	(3.69)	(3.67)	(3.42)	(2.24)
T-Note	-2.4595*	-1.5603*	-1.1035*	-0.9273*	-2.5467*	-1.7185*	-9.5597†	-9.4014†	-4.0206*	-3.3823*	-14.0365*	-13.771*
	(17.84)	(15.68)	(13.09)	(9.83)	(22.00)	(15.20)	(2.40)	(2.43)	(2.72)	(4.26)	(3.18)	(4.43)
Term Slope	-5.5080*	-3.8658*	-2.9417*	-2.6337*	-5.9552*	-4.3546*	-14.0822	-19.6601†	-10.0332*	-10.7150*	-28.8487*	-34.342*
	(18.01)	(15.71)	(14.92)	(11.25)	(23.43)	(16.71)	(1.58)	(2.21)	(2.99)	(5.25)	(2.97)	(3.69)
EuroDollar	-0.0774*	-0.0677*	-0.0560*	-0.0541*	-0.0889*	-0.0751*	0.0328	-0.1369	-0.2440*	-0.3370*	-0.4291*	-0.3924†
	(16.42)	(15.31)	(14.02)	(13.92)	(23.61)	(19.13)	(0.25)	(0.98)	(4.11)	(5.15)	(3.01)	(2.45)
Credit Rating	0.0021*	0.0020*	0.0023*	0.0023*	0.0021*	0.0021*	0.0247*	0.0249*	0.0092*	0.0091*	0.0372*	0.0366*
	(26.96)	(20.14)	(32.54)	(24.35)	(34.62)	(22.55)	(9.61)	(6.45)	(8.67)	(6.85)	(13.25)	(9.29)
$\sigma_E$		3.4437*		5.2107*		4.1768*		4.2847		2.8546†		16.8334*
		(4.99)		(6.85)		(5.32)		(1.92)		(2.27)		(3.86)
PreTax D1		-0.0012*		-0.0015*		-0.0010*		0.0091*		-0.0014		0.0037
		(5.93)		(6.85)		(5.32)		(2.79)		(0.93)		(0.73)
PreTax D2		0.0005*		0.0006*		0.0005*		-0.0103		0.0043†		-0.0051
		(3.56)		(4.83)		(4.33)		(1.46)		(2.12)		(0.85)
PreTax D3		0.0001		0.0002†		0.0001		0.0060		0.0047		0.0138*
		(1.21)		(2.24)		(1.59)		(0.75)		(1.78)		(2.66)
PreTax D4		-0.0001*		-0.0001*		-0.0001		0.0014		-0.0067†		0.0273
		(2.57)		(4.52)		(1.65)		(0.12)		(2.52)		(1.16)
Oper. Inc. to Sales		-0.0069*		-0.0080*		-0.0079*		-0.0185		-0.0277*		-0.0900
		(4.80)		(6.34)		(5.29)		(1.38)		(2.81)		(1.10)
LT Debt to Assets		-0.0057*		-0.0061*		-0.0047†		0.0165		-0.0147		-0.0295
		(3.22)		(3.83)		(2.56)		(0.48)		(0.90)		(0.32)
Total Debt to Cap.		0.0049†		0.0036†		0.0073*		0.0519		0.0748*		0.0185*
		(2.53)		(2.19)		(4.29)		(0.78)		(4.24)		(4.29)
N	5838	2176	6035	2374	8802	3257	1041	461	583	288	1413	606
% Adj. $R^2$	29.19	41.84	25.44	47.91	25.47	46.02	37.04	44.30	32.04	58.36	33.40	44.09
	LOT	Rating	Bid-Ask	Rating	% Zeros	Rating	LOT	Rating	Bid-Ask	Rating	% Zeros	Rating
Coefficient	0.4233*	0.0028*	0.5536*	0.0025*	0.0183*	0.0026*	2.4233*	0.0318*	3.3941*	0.0106*	0.1158*	0.0379*
	(9.67)	(29.82)	(6.36)	(32.67)	(10.96)	(35.00)	(9.07)	(9.89)	(4.77)	(10.17)	(7.14)	(12.35)
% Adj. $R^2$	7.57	15.20	2.12	20.12	3.95	15.08	21.83	24.00	7.49	25.12	3.02	28.21

Table 4

Fixed Effects: Yield Spread Determinant Tests

The yield spread determinants are based on bond-specific effects (bond rating, amount outstanding, and maturity in years), macroeconomic variables (one-year Treasury note rate (T-note), the difference between the 10-year and 2-year Treasury rates (Term Slope), and the 30-day Eurodollar rate minus the 3-month T-Bill Rate (Eurodollar)), and firm-specific operating characteristics (pre-tax interest coverage, operating income to sale, long-term debt to assets, and total debt to capitalization). The pretax interest coverage is further grouped into one of four categories according to Blume et al. (1998).  $\sigma_E$  is the equity volatility for each issuer. Investment grade bonds are numbered from one (AAA rated bonds) to 10 (BBB- rated bonds) Speculative grade bonds are numbered from one (BB+ rated bonds) to 12 (D rated bonds). The liquidity cost proxies include the LOT estimate, the percentage of zero returns, and the bid-ask spread. The issuer is the fixed effect. The issuer fixed effects test is reported by the F-test. An \* or a † signifies significance at the 1% or 5% level, respectively.

Variable	Investment Grade Bonds						Speculative Grade Bonds					
Intercept	0.1111*	0.1194*	0.1086*	0.0932*	0.1219*	0.1053*	0.7743†	0.2208	0.3588*	0.4188*	1.0571*	0.0360
	(12.15)	(14.11)	(14.93)	(10.25)	(10.98)	(13.78)	(2.55)	(0.61)	(2.87)	(3.78)	(3.47)	(0.85)
LOT	<b>0.2118*</b>	<b>0.1078*</b>					<b>2.2897*</b>	<b>0.8764*</b>				
	(13.12)	(9.73)					(13.80)	(4.31)				
Bid-Ask			<b>0.1703*</b>	<b>0.2019*</b>					<b>1.4963*</b>	<b>1.5890*</b>		
			(5.72)	(5.15)					(4.75)	(4.17)		
% Zeros					<b>0.0119*</b>	<b>0.0044*</b>					<b>0.0981*</b>	0.0482
					(13.01)	(5.75)					(5.01)	(1.72)
Maturity	0.0001*	0.0001*	0.0002*	0.0001*	0.0001*	0.0002*	-0.0029*	-0.0029*	-0.0011*	-0.0011*	-0.0022*	-0.0028*
	(5.60)	(12.15)	(12.51)	(12.45)	(9.98)	(14.75)	(4.84)	(4.22)	(7.85)	(7.18)	(3.94)	(3.73)
Amount	-0.0006†	-0.0004	-0.0001	-0.0002	-0.0005*	-0.0003	-0.0058	-0.0026	-0.0064*	-0.0041†	0.0038	0.0087†
	(2.26)	(1.86)	(0.60)	(0.84)	(2.72)	(1.63)	(1.48)	(0.79)	(2.93)	(1.95)	(1.00)	(2.20)
Coupon	0.0658*	0.0705*	0.0005*	0.0005*	0.0629*	0.0667*	0.6891	1.6274*	0.0013	0.0002	0.6689	1.5849*
	(3.84)	(5.32)	(5.10)	(3.84)	(4.83)	(6.03)	(1.28)	(3.09)	(1.00)	(0.17)	(1.31)	(2.62)
T-Note Rate	-1.5298*	-1.2470*	-1.1839*	-0.9141*	-1.6169*	-1.1972*	-13.6442*	-5.8177	-2.4538	-5.3023*	-19.0025*	-10.352
	(17.02)	(18.48)	(15.85)	(10.96)	(19.69)	(17.02)	(3.48)	(1.18)	(1.35)	(3.29)	(4.24)	(1.78)
Term Slope	-3.6526*	-3.3459*	-3.2950*	-2.6766*	-3.9435*	-3.2680*	-20.8069†	-13.1133	-7.5091†	-13.7416*	-39.3252*	-24.667
	(17.60)	(21.05)	(19.81)	(14.15)	(21.16)	(20.08)	(2.42)	(1.20)	(2.04)	(4.18)	(4.59)	(1.92)
Eurodollar	-0.0570*	-0.0602*	-0.0685*	-0.0545*	-0.0637*	-0.0591*	-0.2086	-0.2031	-0.2571*	-0.2533*	-0.6623*	-0.3158
	(15.95)	(20.94)	(25.95)	(17.22)	(21.74)	(21.90)	(1.57)	(1.20)	(7.64)	(6.39)	(5.37)	(1.62)
Credit Rating	0.0035*	0.0008*	0.0009*	0.0008*	0.0031*	0.0012*	0.0048	0.0250*	0.0123*	0.0123*	0.0300*	0.0423*
	(16.98)	(3.87)	(5.92)	(3.75)	(19.03)	(6.28)	(1.25)	(6.52)	(10.37)	(9.80)	(8.36)	(9.67)
$\sigma_E$		1.1266*		2.2140*		1.8186*		-1.5774		-2.9956*		6.8704
		(3.89)		(5.40)		(6.80)		(0.44)		(3.21)		(1.72)
Pre-Tax D1		-0.0013*		-0.0010*		-0.0009*		0.0098		0.0035†		0.0007
		(7.67)		(5.42)		(5.82)		(1.52)		(2.34)		(0.10)
Pre-Tax D2		0.0003†		0.0005*		0.0004*		-0.0045		0.0007		0.0028
		(1.96)		(3.55)		(3.70)		(0.29)		(0.26)		(0.23)
Pre-Tax D3		0.0001		0.0000		0.0001		0.0336		0.0076		0.0057
		(0.47)		(0.27)		(1.11)		(0.66)		(1.26)		(0.30)
Pre-Tax D4		-0.0000		0.0000		-0.0000		-0.0578		-0.0077		-0.0099
		(0.15)		(0.42)		(0.37)		(0.62)		(1.26)		(0.36)
Oper. Inc. to Sales		-0.0022		-0.0068*		-0.0039		-0.0274		-0.0713*		0.0024
		(1.00)		(3.10)		(1.92)		(0.69)		(3.42)		(0.46)
LT Debt to Assets		-0.0004		-0.0047		0.0005		0.0618†		0.0812*		0.0037
		(0.15)		(1.42)		(0.19)		(2.02)		(2.73)		(0.09)
Total Debt to Cap.		0.0187*		0.0182*		0.0186*		0.1041		0.0732*		-0.0094
		(6.79)		(6.33)		(7.60)		(1.25)		(2.79)		(0.12)
Sample Size	5838	2176	6035	2374	8802	3257	1041	461	583	288	1413	606
Issuers	1124	336	1019	306	1235	367	263	96	179	76	294	106
F-Statistic	6.67*	14.01*	14.06*	14.12*	8.74*	15.80	3.06*	2.10*	11.11*	9.65*	3.67*	2.90*

## Table 5

### Simultaneous Regressions

Simultaneous regressions are presented using three liquidity measures, the LOT estimate, the percentage of zero returns, and the bid-ask spread. The liquidity instrumental variables are the bond return volatility, the amount outstanding, the age and maturity in years, and bond rating.  $\sigma_B$  and  $\sigma_E$ , refer to bond volatility and equity volatility, respectively. The amount outstanding and bond volatility are log scaled. The instrumental variables of the yield spread include bond-specific effects (bond rating, amount outstanding, and maturity in years), macroeconomic variables (one-year T-note rate, the difference between the 10-year and two-year Treasury rates, and the 30-day Eurodollar rate over 3-month T-bill rate), and firm-specific accounting variables (pre-tax interest coverage, operating income to sales, long-term debt to assets, and total debt to capitalization), and equity market effects (equity volatility). The instrumental variables of bond rating are the bond age and firm-specific accounting variables. An \* denotes 1% significance while a † denotes 5% significance.

Instrumental Variable	Investment Grade								
	Yield Spread	Bid-Ask	Credit Rating	Yield Spread	LOT	Credit Rating	Yield Spread	%Zeros	Credit Rating
Intercept	0.1661* (2.77)	0.0150* (5.05)	8.4213* (6.52)	0.2398* (5.10)	0.1476* (13.84)	8.1414* (8.39)	0.7819 (1.87)	1.1697* (10.46)	7.9553* (9.12)
Liquidity	<b>7.0442*</b> (4.23)			<b>0.9975*</b> (7.44)			<b>0.2126†</b> (1.96)		
Maturity	-0.0003 (1.94)	0.0001† (2.19)		0.0001 (1.29)	-0.0004* (9.23)		0.0001 (1.72)	-0.0028* (5.88)	
Coupon	-0.0009 (1.14)			-0.0504 (0.66)			-0.1899 (1.93)		
T-Note	-2.5455* (3.41)		-49.4529† (2.35)	-3.9712* (6.55)		-35.4179† (2.32)	-11.8048† (1.96)		-34.8361† (2.50)
Term Slope	-6.7878* (3.82)		-86.3815† (2.08)	-8.6125* (6.93)		-61.5634† (0.31)	-26.2885† (2.00)		-60.4370† (2.17)
Eurodollar	-0.1121* (4.36)			-0.0810* (6.79)			-0.2727† (2.19)		
$\sigma_E$	2.0849 (0.92)			1.6004 (1.88)			-5.2688 (1.43)		
Credit Rating	0.0057† (2.34)	0.0003* (3.18)		0.0056* (2.65)	0.0018* (4.90)		0.0038* (3.94)	0.0396* (9.54)	
PreTax D1	-0.0001 (1.44)		0.0414 (1.15)	-0.0003 (0.81)		0.0140 (0.39)	0.0016 (1.10)		0.0382 (1.29)
PreTax D2	0.0015 (1.66)		-0.2862* (9.67)	0.0015† (2.19)		-0.2921* (9.52)	0.0012 (1.03)		-0.2964* (11.98)
PreTax D3	0.0005 (1.02)		-0.1152* (5.48)	0.0004 (1.51)		-0.1012* (4.20)	0.0001 (1.03)		-0.1031* (5.56)
PreTax D4	-0.0002 (0.81)		0.0337* (3.67)	-0.0001 (0.99)		0.0298* (2.82)	0.0001 (0.31)		0.0226* (2.88)
Operating Income	0.0002 (0.03)		-1.4810* (5.84)	0.0051 (1.02)		-1.7060* (6.41)	0.0079 (1.21)		-1.4883* (6.93)
Long Term Debt to Assets	-0.0282† (2.40)		3.9493* (12.85)	-0.0189 (1.90)		4.0813 (12.76)	-0.0188 (1.28)		3.6651* (14.21)
Total Debt to Cap.	0.0026 (0.44)		-0.1889 (0.58)	0.0077† (2.17)		-0.4549 (1.34)	0.0202† (2.53)		-0.4472 (1.59)
$Ln(\sigma_B)$		0.0008* (5.44)			0.0080* (17.22)			0.0633* (12.76)	
$Ln(\text{Amt. Outstanding})$		-0.0002 (1.80)			-0.0026* (5.79)			-0.0250* (5.53)	
Bond Age		0.0001† (2.45)			-0.0001 (0.58)			-0.0001 (0.04)	
Yield Spread		-0.0784* (3.24)	63.4919* (11.34)		-0.7430* (9.11)	50.2688* (8.78)		-9.9378* (10.83)	56.7310* (12.14)
Sample Size		2374			2176			3257	
Adjusted $R^2$	5.23	5.48	40.05	17.77	13.80	36.88	3.45	5.88	36.45

**Table 5: Continued**  
**Simultaneous Regressions**

Instrumental Variable				Speculative Grade					
	Yield Spread	Bid-Ask	Credit Rating	Yield Spread	LOT	Credit Rating	Yield Spread	%Zeros	Credit Rating
Intercept	0.0139 (0.04)	0.0077 (0.78)	4.9369 (0.75)	0.1265 (0.30)	0.0568* (1.06)	-8.1870 (1.64)	0.4540* (0.66)	-0.7170* (3.02)	-2.8820 (0.51)
Liquidity	<b>12.1308</b> † (1.95)			<b>1.8432</b> † (1.96)			-0.1944 (0.83)		
Maturity	-0.0027† (2.14)	0.0001* (2.72)		-0.0024* (3.89)	0.0008 (1.85)		-0.0039* (3.37)	0.0041† (2.07)	
Coupon	0.0064† (2.35)			0.2784 (1.24)			1.5665* (2.76)		
T-Note	0.4380 (0.08)		-49.1239 (0.45)	-4.5914 (0.82)		192.8104† (2.35)	-4.3845 (0.58)		80.9381 (0.87)
Term Slope	-5.7854 (0.51)		-66.7110 (0.31)	-5.8488 (0.39)		375.1280† (2.29)	-16.1279 (1.00)		165.3930 (0.89)
Eurodollar	-0.5536† (2.65)			0.0981 (0.36)			-0.5329† (2.11)		
$\sigma_E$	5.9458 (1.32)			-0.4133 (0.17)			17.8417† (1.97)		
Credit Rating	0.0321* (3.68)	0.0018* (4.70)		0.0211† (2.04)	-0.0024 (0.79)		0.0397* (3.85)	0.0657* (3.10)	
PreTax D1	0.0090† (2.14)		-0.3952* (6.20)	0.0081 (1.80)		-0.3802* (4.38)	-0.0017 (0.20)		-0.1887† (1.98)
PreTax D2	0.0073 (1.06)		0.0611 (0.49)	0.0078 (0.73)		-0.0868* (0.36)	-0.0170 (0.85)		-0.0784 (0.41)
PreTax D3	-0.0067 (0.64)		-0.1693 (0.92)	-0.0192 (0.81)		-0.0994 (0.21)	0.0194 (0.97)		-0.0460 (0.17)
PreTax D4	-0.0031 (0.26)		0.2538 (1.11)	0.0345 (0.88)		0.1380 (0.18)	-0.0190 (0.80)		0.1594 (1.79)
Operating Income	0.1101 (1.90)		-0.5159 (0.97)	-0.0045 (0.15)		-0.8189 (1.45)	0.0410 (0.69)		-1.3637 (1.79)
Long Term Debt to Assets	-0.1915* (2.84)		2.4873* (3.17)	0.0490 (1.50)		-0.1068 (0.20)	-0.2921* (3.81)		3.2336* (2.89)
Total Debt to Cap.	0.1994* (3.77)		-3.1155* (4.00)	-0.0372 (0.59)		-1.2718 (1.47)	0.1443† (1.96)		-1.4239 (1.45)
$Ln(\sigma_B)$		0.0004 (1.30)			0.0024 (0.65)			-0.0992* (6.38)	
$Ln(\text{Amt. Outstanding})$		-0.0001 (0.11)			-0.0012 (1.06)			-0.0006 (0.09)	
Bond Age		-0.0002† (2.28)			-0.0004 (1.03)			-0.0057 (1.56)	
Yield Spread		-0.0312 (1.59)	24.3250* (9.38)		0.3014* (3.45)	22.3214* (16.65)		0.1582 (0.56)	15.5033* (14.32)
Sample Size		288			461			606	
Adjusted $R^2$	28.81	22.17	58.57	46.46	22.84	47.82	35.31	6.08	36.87



Table 6

Yield Spread Change Determinants and Liquidity Tests

The yield spread change determinants are based on bond-specific effects, macroeconomic effects, and firm-specific operating characteristics. Annual changes in all variables are examined for the 1995-2003 period. The liquidity cost proxies include the LOT estimate, the percentage of zero returns, and the bid-ask spread. We use a cardinal scale for all bonds, regardless of whether they are investment grade or speculative grade bonds, ranging from one for AAA bonds to 22 for D rated bonds. The firm-specific operating characteristics are pre-tax interest coverage, operating income to sales, long-term debt to assets, and total debt to capitalization.  $\sigma_E$  is equity volatility. T-Note Rate is the one-year Treasury rate. Term-Slope is the difference between the 10 year and 2-year Treasury rates. Eurodollar refers to the difference between the 30-day Eurodollar rate and the 3-month T-Bill rate. The last partition is a univariate regression of the yield spread on either liquidity or credit rating alone using only the available bond-specific sample for each liquidity measure. White's (1980) t-statistics are presented in parentheses. An \* denotes 1% significance while a † denotes 5% significance.

Variable	Investment Grade Bonds						Speculative Grade Bonds					
Intercept	-0.0001 (0.49)	-0.0004 (1.34)	-0.0005* (2.81)	-0.0006* (2.80)	-0.0014* (5.49)	-0.0006 (1.83)	0.0327 (2.55)	0.0213 (1.31)	0.0003 (0.08)	0.0080 (1.06)	-0.0103* (10.21)	-0.0006 (0.39)
$\Delta(\text{LOT})$	<b>0.1885*</b> (5.92)	<b>0.1239*</b> (4.01)					<b>1.5153*</b> (3.56)	<b>0.6068*</b> (4.17)				
$\Delta(\% \text{Zero})$			<b>0.0286*</b> (6.02)	<b>0.0134†</b> (3.51)					0.0172 (1.81)	<b>0.0369†</b> (2.11)		
$\Delta(\text{Bid-Ask})$					<b>0.1873†</b> (2.22)	<b>0.2909†</b> (2.34)					<b>2.1636†</b> (2.44)	<b>2.4613†</b> (2.57)
$\Delta(\text{Credit Rating})$	0.0015* (2.64)	0.0011* (2.91)	0.0018* (4.48)	0.0015* (5.10)	0.0007* (4.25)	0.0014* (4.33)	0.0123 (1.90)	0.0293* (4.99)	0.0098* (5.75)	0.0089* (3.03)	0.0181* (6.72)	0.0197* (6.17)
$\Delta(\text{T-Note})$	-0.9791* (13.04)	-0.7426* (9.69)	-1.1166* (11.04)	-0.6589* (7.48)	-0.9203* (12.31)	-0.4271* (4.18)	-8.9819 (2.29)	-6.9540 (1.65)	-4.2911† (2.43)	-2.6598 (0.56)	-0.2080 (0.46)	0.4007 (0.56)
$\Delta(\text{Term Slope})$	-2.6012* (15.60)	-2.2579* (13.90)	-2.7856* (13.24)	-1.9930* (11.41)	-2.5691* (16.15)	-1.5795* (7.72)	-18.153† (2.22)	-20.057† (2.40)	-10.728* (3.12)	9.8818 (0.99)	-1.1486 (1.17)	-3.3099 (1.69)
$\Delta(\text{Euro-Dollar})$	-0.0538* (16.93)	-0.0473* (12.62)	-0.0504* (9.40)	-0.0397* (15.28)	-0.0601* (23.95)	-0.0385* (11.13)	-0.2534 (2.41)	-0.2927† (2.30)	-0.1999* (7.18)	-0.2396* (3.37)	-0.2001* (3.96)	-0.2808* (4.87)
$\Delta(\sigma_E)$		-0.3013 (0.36)		-0.5490 (0.73)		-1.7774 (1.77)		-3.0106 (1.79)		-2.1667† (1.94)		2.2830 (1.21)
$\Delta(\text{PreTax Interest})$		0.0000 (0.08)		0.0001 (1.02)		0.0001 (1.75)		-0.0001 (0.10)		-0.0005 (1.08)		-0.0000 (0.02)
$\Delta(\text{Operating Income})$		-0.0107* (2.57)		-0.0115* (4.01)		-0.0181* (3.12)		0.0044 (0.16)		-0.0192 (1.55)		-0.0393 (0.75)
$\Delta(\text{LT Debt to Assets})$		0.0094 (1.80)		0.0037 (0.97)		0.0189* (3.02)		0.0437 (1.25)		0.0027 (0.09)		0.0709 (0.97)
$\Delta(\text{Debt to Capit.})$		0.0083 (1.67)		0.0075† (2.08)		-0.0057 (0.92)		0.0674 (1.38)		0.0407 (1.54)		0.0349 (0.90)
Sample Size	2646	985	5170	1842	2914	1164	451	198	477	195	188	103
Adj $R^2$ (%)	11.93	21.19	9.10	17.32	16.06	18.34	17.49	63.26	18.98	33.05	34.17	50.43
Liquidity Alone	0.1847 (6.19)		0.0276* (5.95)		0.2270* (2.57)		1.7739* (4.74)		0.0527* (5.57)		0.9534† (2.00)	
% Adj. $R^2$	2.80		2.32		0.19		16.89		5.97		0.75	
Credit Risk Alone	0.0018† (2.53)		0.0023* (4.36)		0.0007* (3.13)		0.0250* (3.56)		0.0095* (4.67)		0.0178* (6.84)	
% Adj. $R^2$	1.03		1.19		0.34		4.30		5.39		19.65	

